

AASHTO T-3 TRIAL DESIGN BRIDGE DESCRIPTION

State: Illinois

Trial Design Designation: IL-4

Bridge Name: _____

Superstructure Type: Simply supported PPC-I beam composite with concrete deck

Span Length(s): 4@43.5 ft. (total 174.0 ft.)

Substructure Type: Pier wall supported on pile cap at bents

Foundation: Steel piles at abutments and bents

Abutments: Seat type supported on steel piles

Seismic Design Category (SDC): "C" _____

Seismic Design Strategy (Type 1, 2 or 3): Type 1

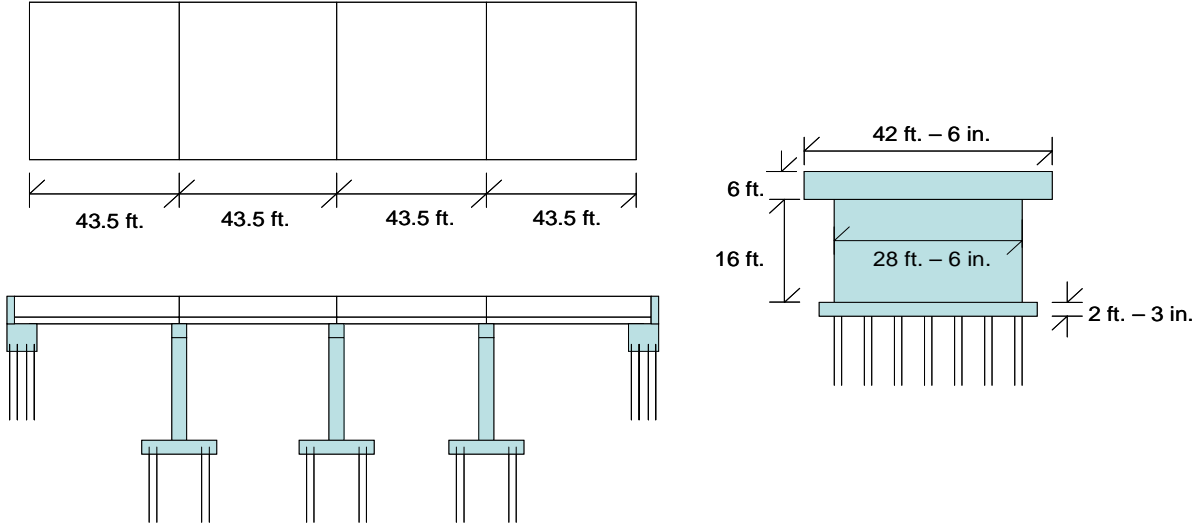
Design Spectral Acceleration at 1-second Period (S_{D1}): 0.487g

Additional Description (Optional): _____

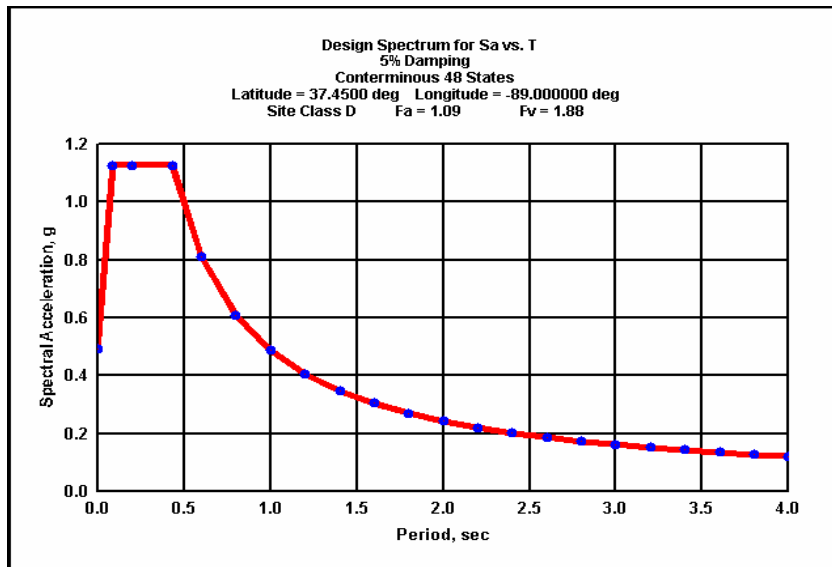
Bridge No.: 4 **Transverse Seismic Calculations**

Description: 4-Span PPC-I Beam with Wall Piers and Steel Piles at Piers and Abutments
(No Skew)

(Pile Design Method Similar for Imbsen and LRFD, therefore not shown - See Bridge No. 2)



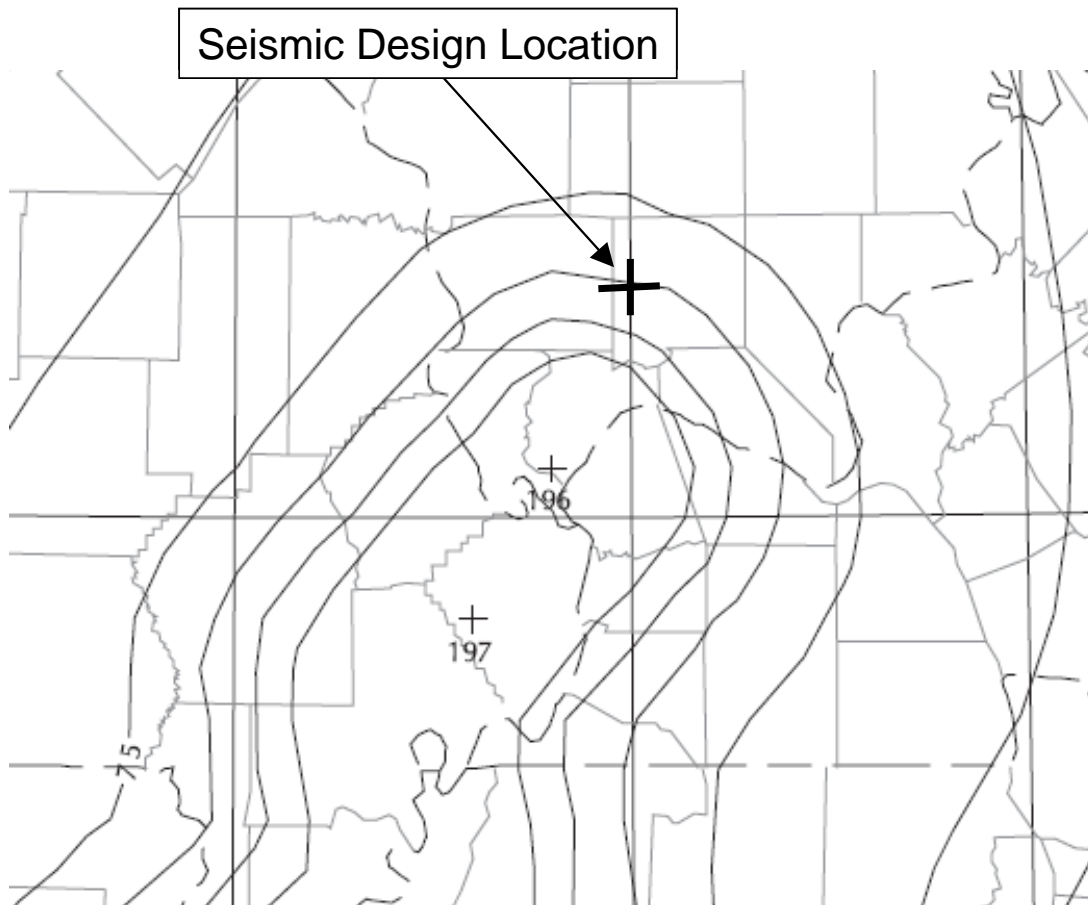
Design Response Spectrum



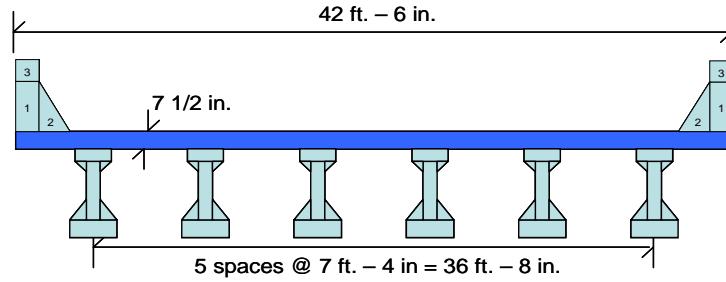
SDC and Other Pertinent Design Spectrum Information

$S_{D1} =$	0.487 g	Seismic Design Category C 0.3g \leq 0.487g $<$ 0.5 g (Imbsen Table 3.5-1)
$S_{DS} =$	1.128 g	
End		
Plateau	0.432 Seconds	

Chosen Location for Bridge Study and 0.2 Second 1000 year Acceleration Map (2006 Map)



Simple Cross Section of Deck

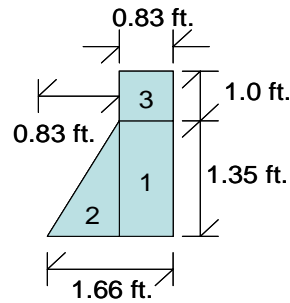


Weight of Super and Sub Structure for Seismic Calculations

Beams	36 in PPC I
No. Beams	6.00
Beam Spacing	7.33 ft.
Wt. of 1 Beam	0.37 k/ft.
Wt. Tot. Beams	2.23 k/ft.

Th. of Slab	7.50 in.
Th. of Surface	0.00 in.
Width	42.50 ft.
Wt. of Slab	3.98 k/ft.

Parapet	
Area 1	1.12 ft ²
Area 2	0.56 ft ²
Area 3	0.83 ft ²
Total Area	2.51 ft ²
Wt. of Parapet	0.38 k/ft.

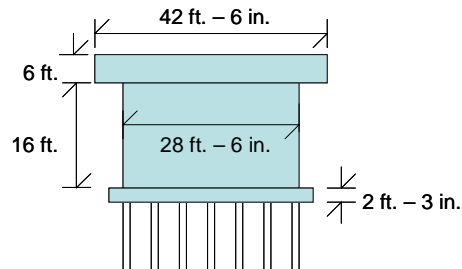


Pier Diaph.	
No. of Diaphr.	3.00
Width	1.83 ft.
Total Weight	105.19 kips

Height	3 ft.
Length	42.5 ft.

Steel Parapet	
Rail	
(est. as	0.00 %
0.02 k/ft)	0.02 k/ft

Cap Beam	
Length	42.50 ft.
Width	2.50 ft.
Height	6.00 ft.
Wt. of 1 Beam	95.63 kips
Wt. of 3 Beams	286.88 kips



Weight of Super and Sub Structure for Seismic Calculations (Cont.)

3 ft. of walls		
Width	28.50 ft.	Thickness 2.50 ft.
Height	3.00 ft.	
Wt. of 1Wall	32.06 kips	
No. of Walls	3	
Wt. of 3 Walls	96.19 kips	
Total Wt. for Seismic Calculations		
Super Length	174 ft.	
Total Weight	1704 kips	

Transverse Period Calculation

Pier Piles Stiffness (Wall is Rigid)	$k_p = \frac{12 \times E_s \times I_s}{h_c^3}$
Pile Type	HP 8 x 36
E_s	29000 ksi
I_s	40 in ⁴
No. Piles	14
h_c	61.2 inches (depth of fixity)
k_p	61 k/in
k_{pier}	852 k/in

I of Super-
structure
Transverse

E_c Prestressed	4031 ksi	
f'_c	3500 psi	
E_c	3372 ksi	
n (mod. Ratio)	1.20	$Area_{ConcBm} = \frac{n \times Area}{2}$ Transf. Area with 50% Shear Lag
I_{slab}	82906875 in ⁴	
Area _{Parapet}	361.4 in ²	
Area 1 Beam	357 in ²	
Area _{Conc Bm}	213.4 in ² (Transformed)	

Transverse Period Calculation (Cont.)

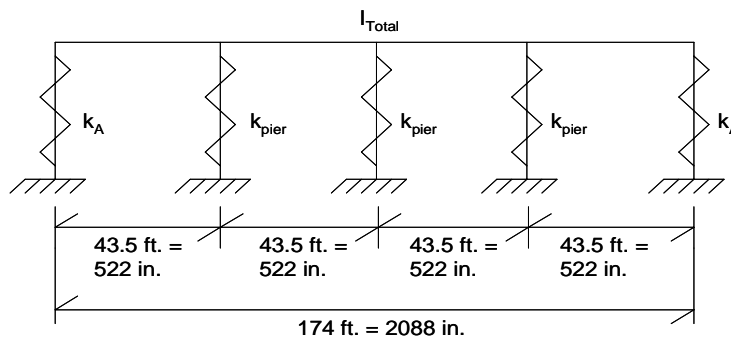
Momen of Inertia of Superstructure Table

	No.	I_0 (In ⁴)	A (in ²)	x bar (in)	A (x bar) ² (in ⁴)	I (in ⁴)
Parapet	2	----	361.44	243	21342670.56	42685341.1
Slab	1	82906875	----	----	82906875	82906875
Steel 1	2	----	213.4	44	413092.6747	826185.349
Steel 2	2	----	213.4	132	3717834.072	7435668.14
Steel 3	2	----	213.4	220	10327316.87	20654633.7

$$I_{Total} = 1.545E+08 \text{ in}^4$$

$$A_{Total} = 5828 \text{ in}^2$$

Model the Bridge Transversely with I_{total} of the Superstr. and Springs for the Abutment Piles and Pier Cols.



Estimate the Abutment Pile Transverse Stiffness

$$k_A = 450 \text{ k/in}$$

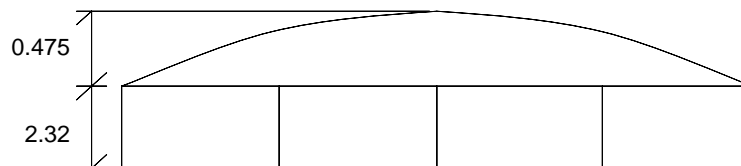
Solve for the Displacement from Simple Model Above as Outlined Below for a 1 k/in Uniform Load

Find the Deflection at the Center of the Bridge Assuming No Piers and Infinitely Stiff Abutments

w	1 k/in	$\delta_C = \frac{5 \times w \times L^4}{384 \times E_c \times I_{Total}}$
L	2088 in	
E_c	3372 ksi	
I_{Total}	1.545E+08 in ⁴	
δ_C	0.475 in	

Find the Deflection Along the Bridge Assuming an Infinitely Stiff Superstr., No Piers, and Abut. Springs

w	1 k/in	$\delta_e = \frac{w \times L}{2 k_A}$
L	2088 in	
k_A	450 k/in	
δ_e	2.32 in	

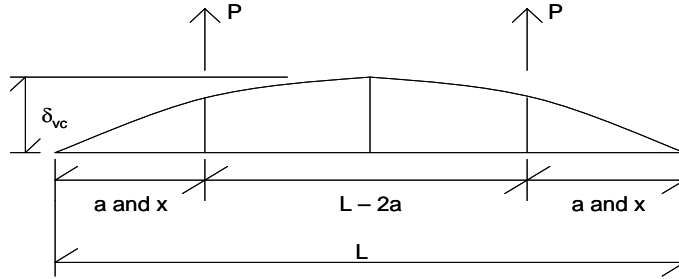


Transverse Period Calculation (Cont.)

Find the Total Estimated Displacement Without the Piers

$$\delta_T = \delta_c + \delta_e \quad 2.795 \text{ in}$$

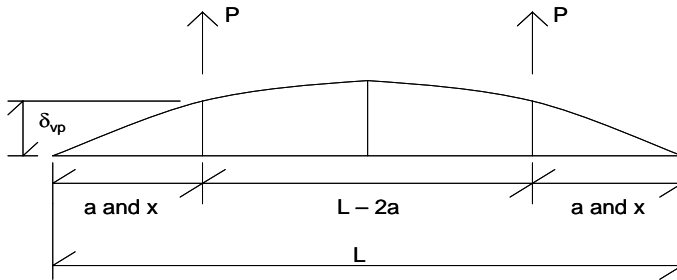
Find the Estimated Deflection at the Center of the Bridge for a Two Point Load at Piers with Infinitely Stiff Abuts. In Terms of an Applied Load "P".



L	2088 in
x	522 in
a	522 in
E _c	3372 ksi
I _{Total}	1.545E+08 in ⁴
δ _{vc}	0.0005005 P

$$\delta_{vc} = \frac{P \times a}{24 \times E_c \times I_{Total}} (3 \times L^2 - 4 \times a^2)$$

Find the Estimated Deflection at the Pier of the Bridge for a Two Point Load at Piers with Infinitely Stiff Abuts. In Terms of an Applied Load "P".

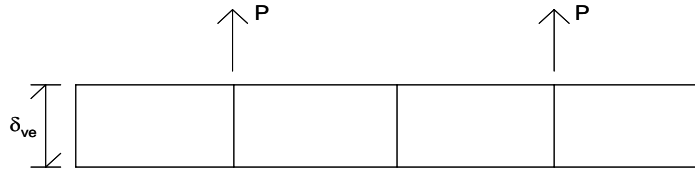


L	2088 in
x	522 in
a	522 in
E _c	3372 ksi
I _{Total}	1.545E+08 in ⁴
δ _{vp}	0.0003640 P

$$\delta_{vp} = \frac{P \times x}{6 \times E_c \times I_{Total}} (3 \times L \times a - 3 \times a^2 - x^2)$$

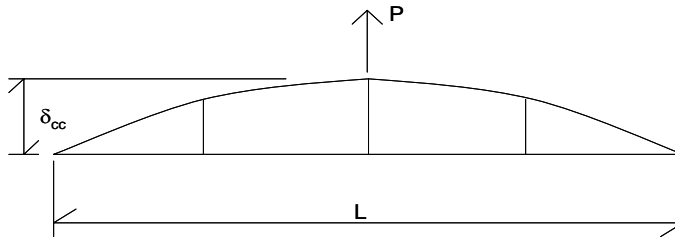
Transverse Period Calculation (Cont.)

Find the Estimated Uniform Deflection for a 2 Point Load at Piers with Springs at Abuts.
In Terms of an Applied Load "P".



k_A	450 k/in	$\delta_{ve} = P/k_A$
δ_{ve}	0.00222222 P	

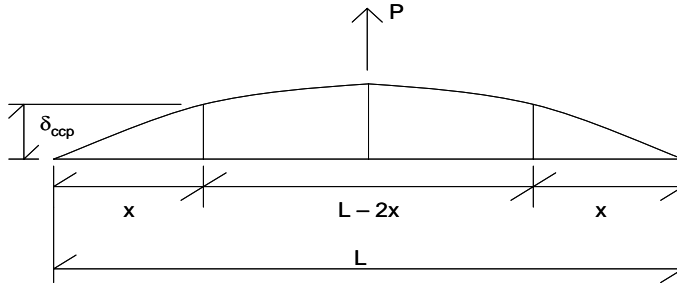
Find the Estimated Deflection at the Center of the Bridge for a 1 Point Load at Piers with Infinitely Stiff Abuts.
In Terms of an Applied Load "P".



L	2088 in	$\delta_{cc} = \frac{P \times L^3}{48 \times E_c \times I_{Total}}$
E_c	3372 ksi	
I_{Total}	1.545E+08 in ⁴	
δ_{cc}	0.0003640 P	

Transverse Period Calculation (Cont.)

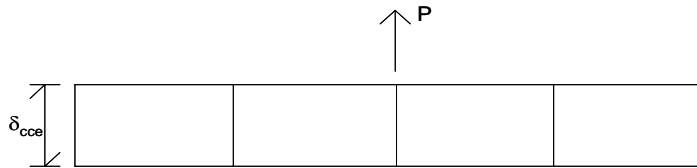
Find the Estimated Deflection at the Outer Piers of the Bridge for a 1 Point Load at Center Pier with Infinitely Stiff Abuts. In Terms of an Applied Load "P".



L	2088 in
x	522 in
E _c	3372 ksi
I _{Total}	1.545E+08 in ⁴
δ _{ccp}	0.0002502 P

$$\delta_{ccp} = \frac{P \times x}{48 \times E_c \times I_{Total}} (3 \times L^2 - 4 \times x^2)$$

Find the Estimated Uniform Deflection for a 1 Point Load at Piers with Springs at Abuts. In Terms of an Applied Load "P".



k _A	450 k/in
δ _{cce}	0.00111111 P

$$\delta_{cce} = \frac{P}{2 \times k_A}$$

Find the Fraction of the Estimated Pier Deflection at the Outer Piers Versus that at Center Span

δ _{vc}	0.0005005 P
δ _{vp}	0.0003640 P
δ _{cc}	0.0003640 P
δ _{ccp}	0.0002502 P
δ _{ve}	0.00222222 P
δ _{cce}	0.00111111 P
fr	0.940

$$fr = \frac{\delta_{ve} + \delta_{cce} + \delta_{vp} + \delta_{ccp}}{\delta_{ve} + \delta_{cce} + \delta_{vc} + \delta_{cc}}$$

Transverse Period Calculation (Cont.)

Find the Outer Pier Reactions (V_0) in Terms of δ_{max} , the Actual Estimated Deflection of the Bridge

fr	0.940	
k_{pier}	852.3 k/in	$V_{00p} = fr \times \delta_{max} \times k_{pier}$
V_{00p}	$801.5 \delta_{max}$	

Find the Center Pier Reaction (V_0) in Terms of δ_{max} , the Actual Estimated Deflection of the Bridge

k_{pier}	852.3 k/in	$V_{00c} = \delta_{max} \times k_{pier}$
V_{00c}	$852.3 \delta_{max}$	

Solve for δ_{max} :

$$\delta_{vc} + \delta_{cc} + \delta_{ve} + \delta_{cce} = 0.004198 P$$

Or (splitting up deflection components)

$$\delta_{vc} + \delta_{ve} = 0.002723 P$$

$$\delta_{cc} + \delta_{cce} = 0.001475 P$$

Set:

$$P = V_{00p} = 801.5 \delta_{max}$$

$$P = V_{00c} = 852.3 \delta_{max}$$

Therefore:

$$\delta_{vc} + \delta_{ve} = 0.002723 \times 801.5 \times \delta_{max}$$

$$\delta_{vc} + \delta_{ve} = 2.182253 \delta_{max}$$

$$\delta_{cc} + \delta_{cce} = 0.001475 \times 852.3 \times \delta_{max}$$

$$\delta_{cc} + \delta_{cce} = 1.257242 \delta_{max}$$

And:

The Actual Estimated Deflection of the Bridge is the Deflection Without Piers Minus the Contribution with the Piers

$$\delta_{max} = \delta_T - 2.182253 \delta_{max} - 1.257242 \delta_{max}$$

$$\delta_{max} = 2.795 / 4.439495$$

$$\delta_{max} = 0.630 \text{ in}$$

Transverse Period Calculation (Cont.)

Solve for the "Equivalent Stiffness" of the Bridge in the Transverse Direction

w	1 k/in	$k_{\text{Bridge}} = \frac{w \times L}{\delta_{\text{max}}}$
L	2088 in	
δ_{max}	0.630 in	
k_{Bridge}	3317 k/in	

Solve for the Period T

Tot. Weight (W)	1704 kips	$T = 2\pi \sqrt{\frac{W}{g \times k_{\text{Bridge}}}}$
g	386.4 in/sec ²	
k_{Bridge}	3316.510 k/in	
T	0.23 seconds	

Transverse Seismic Force On Superstructure (Base Shear)

0.23 < 0.432 seconds

Therefore: 112.8% of the Mass is "Effective" and the Total Seismic Load in the Transverse Direction is:

1.128 x 1704 = 1923 kips (Base Shear)

or:
1923 / 2088 = 0.92 k/in (Base Shear)

Transverse Seismic Force on Outer Piers (Base Shear)

$V_{\text{Base Shear P}} = 0.92 / 1 \times 0.630 \times 801.5$

$V_{\text{Base Shear P}} = 465 \text{ kips}$

Transverse Seismic Force on Center Pier (Base Shear)

$V_{\text{Base Shear P}} = 0.92 / 1 \times 0.630 \times 852.3$

$V_{\text{Base Shear P}} = 494 \text{ kips}$

Transverse Seismic Force on Abutments (Base Shear)

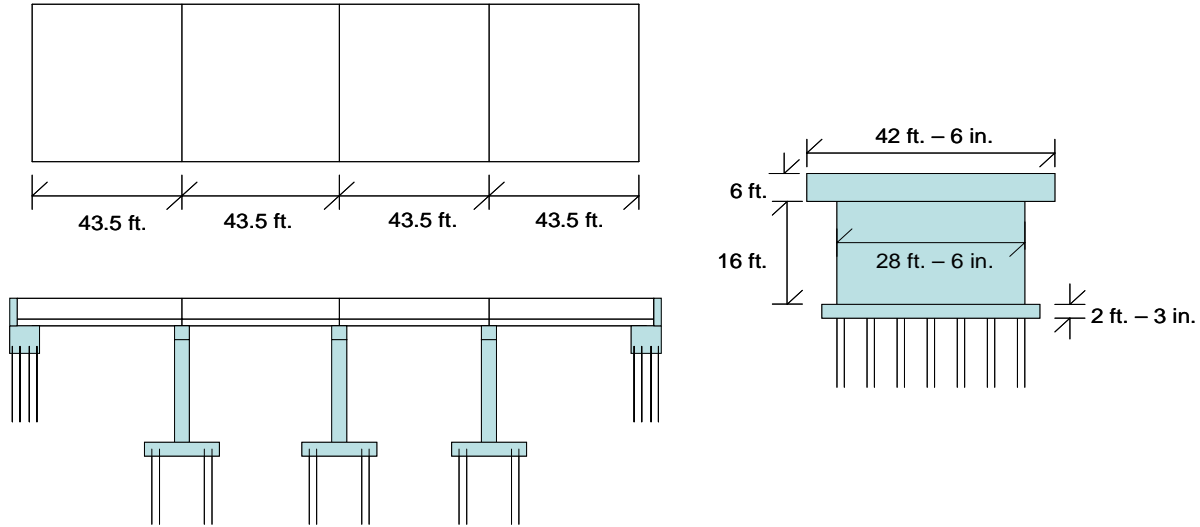
$V_{\text{Base Shear A}} = 1923 - 929.25248 - 494 / 2$

$V_{\text{Base Shear A}} = 250 \text{ kips}$

Transverse Seismic Displacement of Center Pier

$\delta_{\text{PierT}} = 494 / 852 = 0.58 \text{ in.}$

Bridge No.: 4 **Longitudinal Seismic Calculations**
 Description: 4-Span PPC-I Beam with Wall Piers and Steel Piles at Piers and Abutments
 (No Skew)



Weight of Superstructure

Total Weight 1704 kips

Longitudinal Period Calculation

Pier Stiffness
 Longitudinal
 Direction

$$k_c = \frac{3 \times E_c \times I_c}{h_c^3}$$

$$E_c = \frac{57000 \sqrt{f'_c}}{1000}$$

$$\theta_{TC} = \frac{P \times h_c^2}{2 \times E_c \times I_c}$$

Contribution from Column

f'_c	3500 psi	
E_c	3372 ksi	
Width	28.50 ft	Thickness 2.5 ft.
I_c	769500 in ⁴	
$I_c/2$	384750 in ⁴	Half Cracked Section
No. Walls	1	
$1 \times I_c/2$	384750 in ⁴	Half Cracked Section
h_c	192 inches (clear column height)	
k_c	550 k/in	
k_{pier}	550 k/in	

Contribution from Cap Beam (Stiffness is infinite but it deflects as a rigid body and contributes to pier stiffness)

Find the estimated deflection at the top of column for a load "P"

$$\delta_{TC} = \frac{P}{550} \text{ in}$$

Find the estimated rotation at the top of column for a load "P"

$$\theta_{TC} = \frac{P}{70390.7} \text{ radians}$$

Cap height 72 in

Find the added estimated deflection at the top of the pier

$$\delta_A = \text{Cap hght} \times \theta_{TC} = \frac{P}{977.6} \text{ in}$$

Find the total estimated deflection at the top of the pier

$$\delta_{TD} = \delta_A + \delta_{TC} = \frac{P}{352.0} \text{ in}$$

So, the stiffness of a pier is:

$$k_{\text{pier}} = 352 \text{ k/in}$$

Find the Mass of the Superstructure

$$M = \frac{1704}{386.4} = 4.41 \text{ k-sec}^2/\text{in}$$

Find the period T:

$$T = 0.41 \text{ sec.} \quad T = 2\pi \sqrt{\frac{M}{3 \times k_{\text{pier}}}}$$

Longitudinal Seismic Force On Superstructure (Base Shear)

$$0.41 < 0.432 \text{ Seconds}$$

Therefore: 112.8% of the Mass is "Effective" and the Total Seismic Load in the Longitudinal Direction is:

$$1.128 \times 1704 = 1923 \text{ kips (Base Shear)}$$

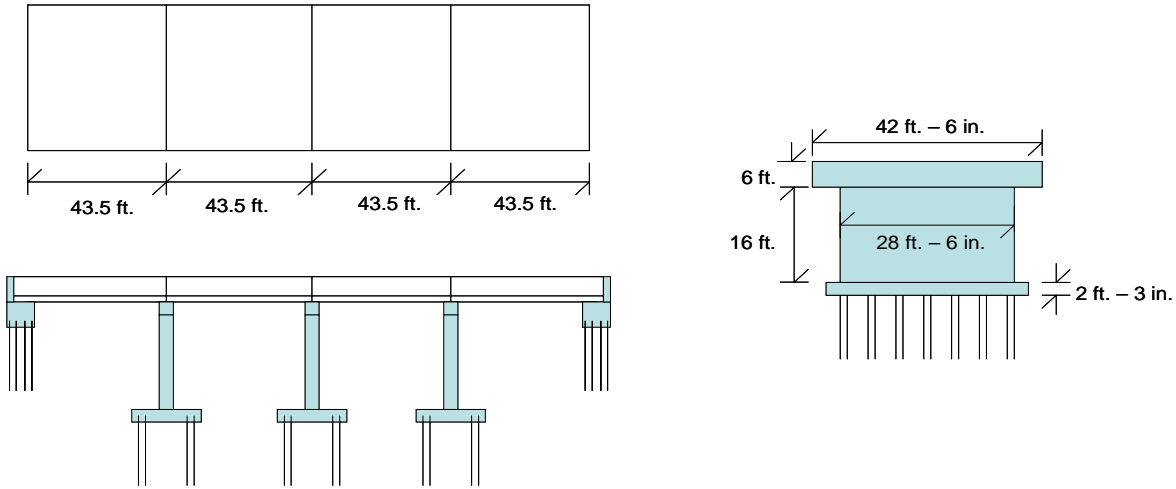
Longitudinal Seismic Force On Each Pier assuming the abutments don't contribute (Base Shear)

$$1923 / 3 = 641 \text{ kips (Base Shear)}$$

Longitudinal Seismic Displacement of Pier

$\delta_{\text{PierL}} =$	641	/	352.0	=	1.82 in.
---------------------------	-----	---	-------	---	----------

Bridge No.: 4 **Force Based Wall Design and Displacement Check**
 Description 4-Span PPC-I Beam with Wall Piers and Steel Piles at Piers and Abutments
 (No Skew)



Center Wall Forces

Dead

Dead Load Total	1704 kips
Bridge Length	436.3 ft.
Dead Load per ft.	3.91 k/ft
Dead Load Ctr. pier	169.9 kips
No. of Walls	1
Dead Ld. Ctr. Wall	169.9 kips
Plus Remaining Wall	138.9 kips
Design Dead	308.9 kips

Transverse Shear and Moment (Simple Cantilever/Shear Wall Statics)

S_p (Pier Base Shear)	494 kips
Col arm (h)	22.00 ft.
$M_{WallBot}$	10869.8 k-ft.

Longitudinal Shear and Moment (Simple Cantilever Statics)

S_L (Pier Base Shear)	641 kips
Col arm (h)	22.00 ft.
$M_{WallBot}$	14098.8 k-ft.

Orthogonally Combined Load Cases

Transverse Dominant - Load Case 1

$$\begin{aligned}
 P &= 308.9 \text{ kips} \\
 M_T &= 10869.8 / 1.5 \text{ (R-factor)} = 7247 \text{ k-ft} \\
 M_L &= 14098.8 / 1.5 \text{ (R-factor)} \times 0.3 = 2820 \text{ k-ft} \\
 M_{\text{Combined}} &= 7776 \text{ k-ft} \\
 \lambda &= \tan^{-1}(M_T/M_L) = 68.7 \text{ degrees}
 \end{aligned}$$

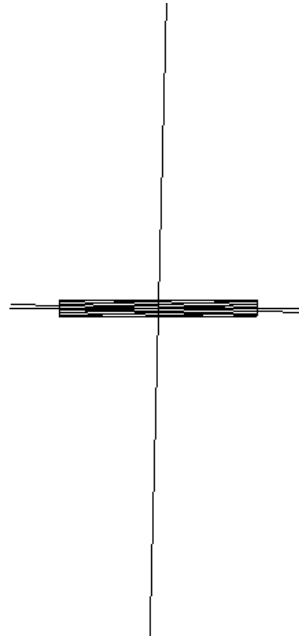
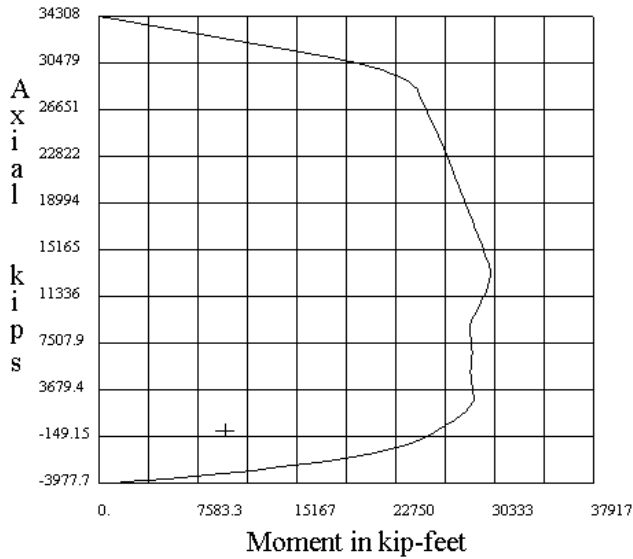
Longitudinal Dominant - Load Case 2 - Governs the Design

$$\begin{aligned}
 P &= 308.9 \text{ kips} \\
 M_T &= 10869.8 / 1.5 \text{ (R-factor)} \times 0.3 = 2174 \text{ k-ft} \\
 M_L &= 14098.8 / 1.5 \text{ (R-factor)} = 9399 \text{ k-ft} \\
 M_{\text{Combined}} &= 9647 \text{ k-ft} \\
 \lambda &= \tan^{-1}(M_T/M_L) = 13.0 \text{ degrees} \\
 \theta &\equiv 0.5 - 1.5 \text{ degrees}
 \end{aligned}$$

Wall Vertical Reinforcement Design - "Nominal Provided"

Pier is Adequate with or without R-Factors Applied (i.e. "not as a ductile or seismic column")

Seismic Rectangular Wall Pier Design



Vertical Reinforcement

Bars: #8
 No. 84
 No. Transverse Faces 39
 No. Longitudinal Faces 5
 $\rho_v = 0.0072 > 0.0025$ (LRFD 5.10.11.4.2 and Imbsen 8.17 - Provisions are Identical)

Displacement Check

We interpret this as a way to check deflections for walls. Imbsen provisions are either somewhat incomplete or unclear on this.

Scratch Calculation Table

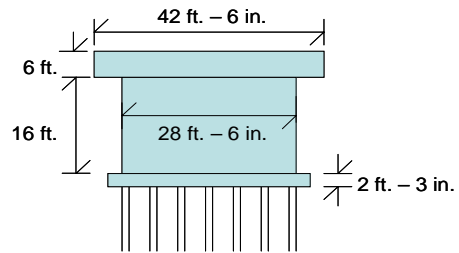
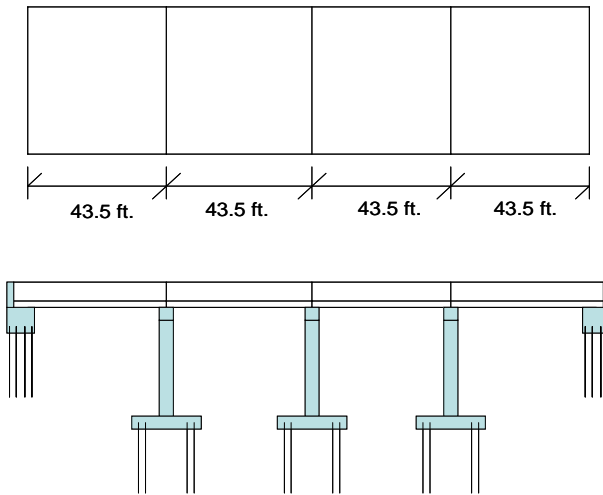
Imbsen Section 4.8					
Wall Height	Wall Width	H/100	x Fixed-Pinned	Delta Calc. Fixed - Pinned	Delta Allow. Fixed - Pinned
(ft)	(ft)	(in)		(in)	(in)
22	2.50	2.64	0.11	10.10	10.10

Longitudinal Direction

Wall Height (ft.)	Imbsen Fig. 5.4		Long. Period (Sec.)	Long. Deflection (in)	Long. Allowable Deflection (in)
	Steel Ratio (Ast/Ag)	Fraction of Ig			
22	0.0072	?	0.41	1.82*	10.10

*Even Amplified per Imbsen 4.3.3 will be OK

Bridge No. 4 **Design for Shear**
 Descriptor 4-Span PPC-I Beam with Wall Piers and Steel Piles at Piers and Abutments
 (No Skew)



Transverse Shear

S_p (Pier Base Shear) 494 kips

Longitudinal Shear

S_L (Pier Base Shear) 641 kips

Orthogonally Combined Load Cases (Elastic)

Transverse Dominant - Load Case 1

$S_{Combined} =$ 530 kips

Longitudinal Dominant - Load Case 2

$S_{Combined} =$ 658 kips

Shear Strength

LRFD 5.10.11.4.2 and Imbsen 8.8.3 are Identical
Check to see that Minimum Shear Reinforcement is Adequate

Take the Lesser of:

$$V_r = 0.253\sqrt{f'_c}bd = 4771 \text{ kips}$$

or

$$V_r = 0.9\left[0.063\sqrt{f'_c} + \rho_h f_y\right]bd = 2430 \text{ kips}$$

Minimum reinforcement is Adequate.

ρ_h set to:	minimum of 0.0025
b set to	30 in
d set to	336 in
f'_c	3.5 ksi
f_y	60 ksi

A "short" spacing of bars may be used near the base of wall if confinement or plastic hinging is a potential concern in the longitudinal direction.

Bridge No.: 4 **Seat Width Requirements**
 Description 4-Span PPC-I Beam with Wall Piers and Steel Piles at Piers and Abutments
 (No Skew)

Seat Width Requirements

Compare Imbsen with NCHRP 12-49 and the Current LRFD Code
 LRFD calibrated for 500 years and 12-49 calibrated to 1.0 Sec. Accel. with improved Soil Coef.
 so it is "return period independent".

NCHRP 12-49
$$N = \left[0.10 + 0.0017L + 0.007H + 0.05\sqrt{H} \sqrt{1 + \left(2\frac{B}{L}\right)^2} \right] (1 + 1.25F_v S_1) \quad (\text{metric})$$

L = 174 ft or 53.04 meters
 FvS1 = 0.487 g
 H = 22 ft or 6.71 meters
 B = 42.5 ft or 12.95 meters

Imbsen 4.12.2
$$N = (4 + \Delta_{ot} + 1.65\Delta_{eq}) \geq 12$$

$\Delta_{ot} = 0.01L = 1.74$ inches
 $\Delta_{eq} = 3^*$ inches
 *Estimated Amplified

LRFD 4.7.4.4
$$N = 8 + 0.02L + 0.08H$$

L = 174 ft %N for Cat. C = 150
 H = 22 ft

Summary of Seat Width Requirements (NCHRP 12-49, Imbsen and LRFD) for 16 Cases

Wall Height (ft.)	Imbsen Fig. 5.4		Long. Deflection (in)	Imbsen 4.12.2	Imbsen 4.12.2	NCHRP 12-49	Current LRFD
	Steel Ratio (Ast/Ag)	Fraction of Ig		Calc. Seat (in)	Req. Seat (in)	Req. Seat (in)	Req. Seat (in)
22	0.0072	?	3.00	11.0	12.0	24.1	19.9